



# Paper Review

Lu, Hong 2020.8



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- Distributed Collision-Avoidance Formation Control: A Velocity Obstacle-Based Approach
- Distributed Lyapunov-based model predictive control for collision avoidance of multi-agent formation
- A General Approach to Coordination Control of Mobile Agents With Motion Constraints

# ON SEGREGATIVE BEHAVIORS USING FLOCKING AND VELOCITY OBSTACLES [2012 DARS]

- Purpose
  - Swarm navigation combining **hierarchical abstractions**, **flocking** behaviors, and an **efficient collision avoidance mechanism**
- Methodology
  - Introducing penalty function to allow to select velocity belonging to VO.
  - Parameter triples  $(\alpha, \beta, w)$

$$\mathbf{v}_i^{\text{flock}} = \mathbf{v}_i^{\text{pref}} + \alpha(\mathbf{v}(\Phi_k) - \mathbf{v}_i) + \beta(\mathbf{p}(\Phi_k) - \mathbf{p}_i)$$

$$P_i(\mathbf{v}'_i) = \frac{w}{c_i(\mathbf{v}'_i)} + \|\mathbf{v}_i^{\text{flock}} - \mathbf{v}'_i\|,$$

$$\mathbf{v}_i^{\text{new}} = \underset{\mathbf{v}'_i \in S}{\operatorname{argmin}} P_i(\mathbf{v}'_i)$$

- **Drawback**

- The same behavior cannot be guaranteed with small sensing neighborhood.

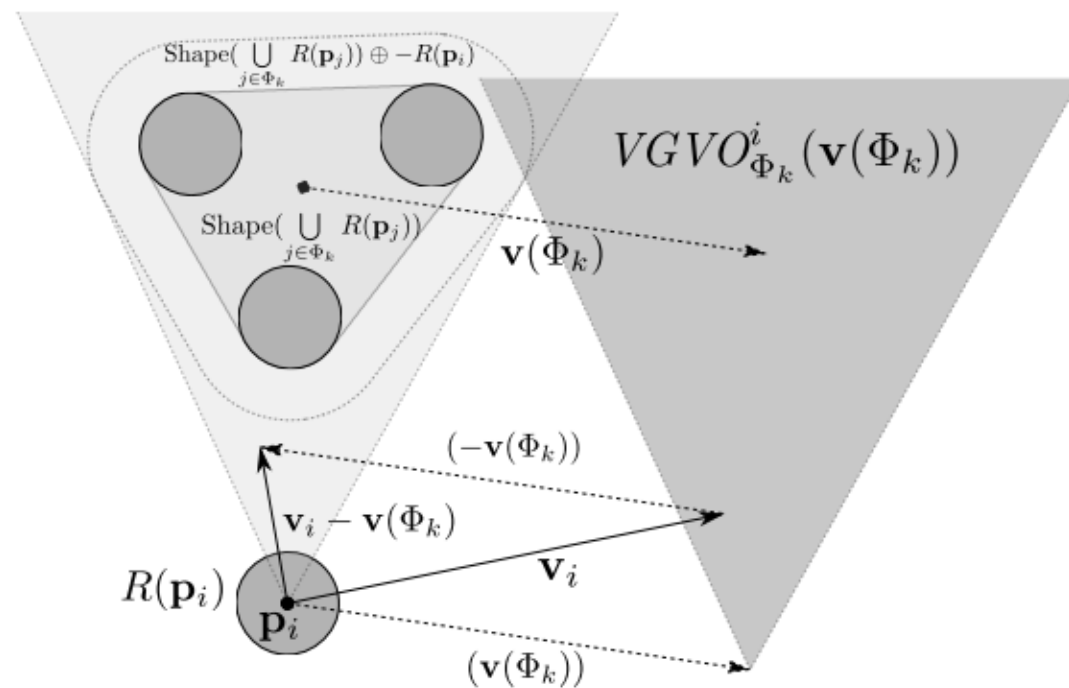
- **Improvement**


- VGVO (virtual group)

$$VGVO_{\Phi_k}^i(\mathbf{v}(\Phi_k)) = \{\mathbf{v}'_i \mid \lambda(\mathbf{p}_i, \mathbf{v}'_i - \mathbf{v}(\Phi_k)) \cap C(\mathbf{p}_i, \Phi_k) \neq \emptyset\},$$

$$C(\mathbf{p}_i, \Phi_k) = \text{Shape}\left(\bigcup_{j \in \Phi_k} R(\mathbf{p}_j)\right) \oplus -R(\mathbf{p}_i),$$

$$VGRVO_{\Phi_k}^i(\mathbf{v}(\Phi_k), \mathbf{v}_i) = \{\mathbf{v}''_i \mid 2\mathbf{v}''_i - \mathbf{v}_i \in VGVO_{\Phi_k}^i(\mathbf{v}(\Phi_k))\}.$$





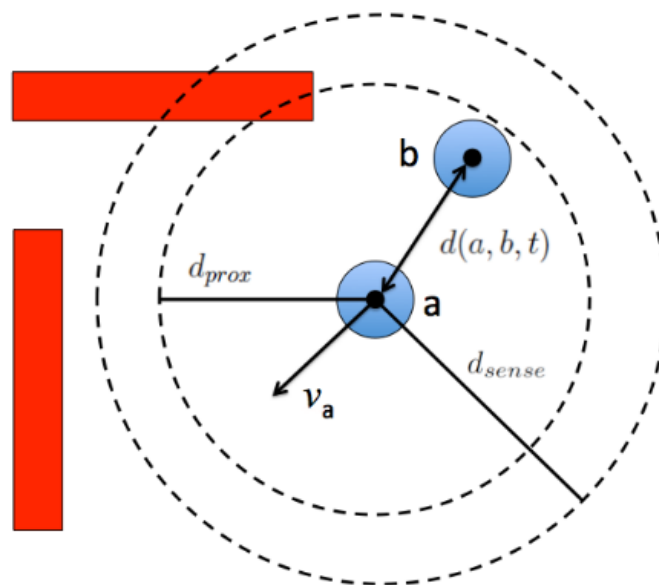
# On Segregative Behaviors Using Flocking and Velocity Obstacles

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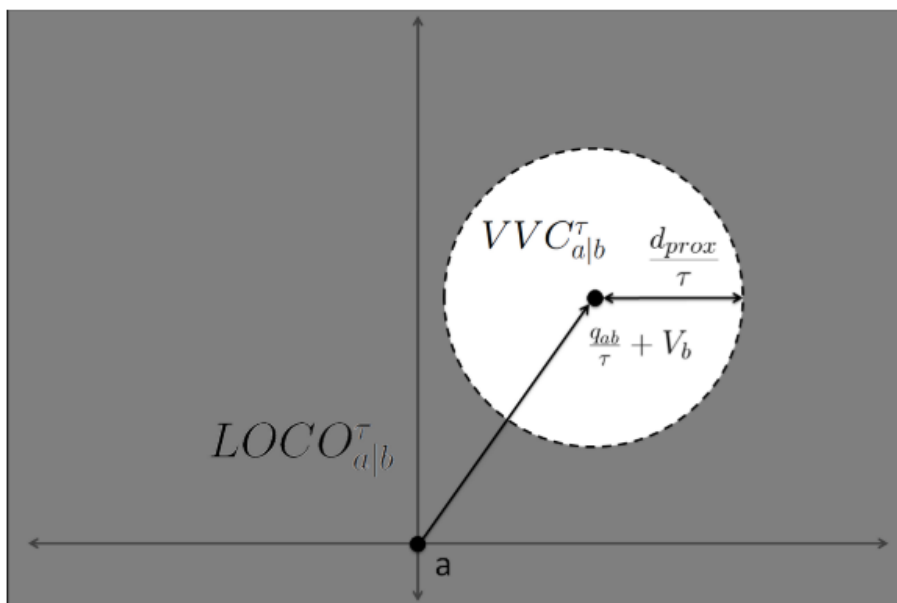
# MAINTAINING TEAM **COHERENCE** UNDER THE VELOCITY OBSTACLE FRAMEWORK [2012 AAMAS]

- Purpose
  - Loss of Communication Obstacle, aiming to maintain proximity among agents by imposing constraints in the velocity space and restricting the set of feasible controls.



# LOCO CONSTRUCTION

- To be noted,  $\tau$  is tuned through comparison between  $V_{valid}$  and  $V_{threshold}$ 
  - $\text{norm}(V_{valid}) < \text{norm}(V_{threshold})$ , time horizon  $\tau$  decreased;
  - Otherwise.



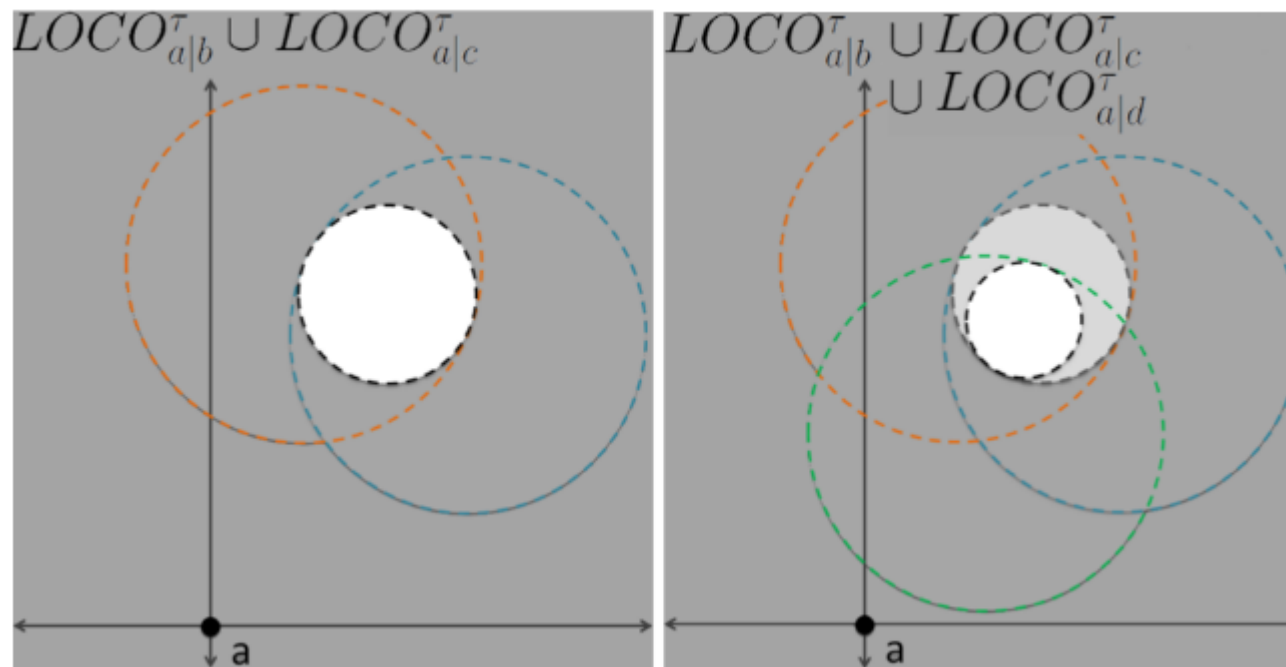
$$(q_{ab}^X(t + \tau))^2 + (q_{ab}^Y(t + \tau))^2 \leq d_{prox}^2 \Rightarrow$$

$$(q_{ab}^X(t) + \tau * (V_b^X - V_a^X))^2 + (q_{ab}^Y(t) + \tau * (V_b^Y - V_a^Y))^2 \leq d_{prox}^2 \Rightarrow$$

$$\left(\frac{q_{ab}^X(t)}{\tau} + V_b^X - V_a^X\right)^2 + \left(\frac{q_{ab}^Y(t)}{\tau} + V_b^Y - V_a^Y\right)^2 \leq \frac{d_{prox}^2}{\tau^2} \Rightarrow$$

$$\left(V_a^X - \frac{q_{ab}^X(t)}{\tau} - V_b^X\right)^2 + \left(V_a^Y - \frac{q_{ab}^Y(t)}{\tau} - V_b^Y\right)^2 \leq \left(\frac{d_{prox}}{\tau}\right)^2$$

# CONSERVATIVE APPROXIMATION



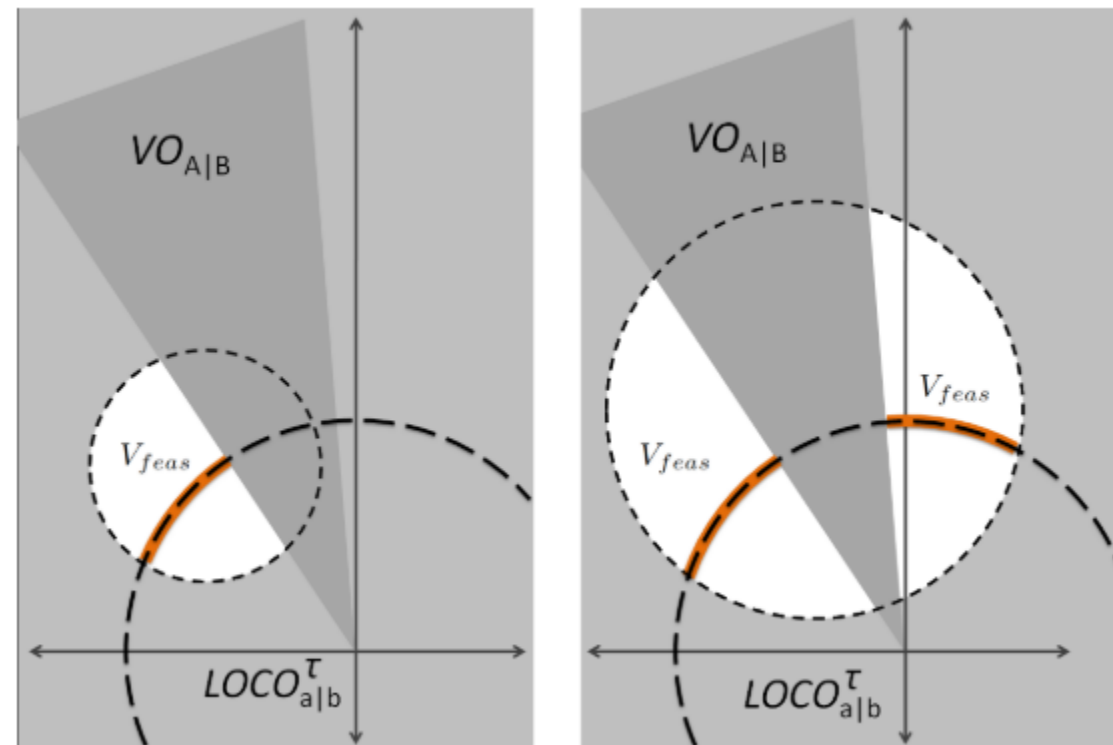


# INTEGRATION

- Weighted velocity selection

$$q_{avg} = \frac{\sum_i^n \frac{d_i}{d_{prox}} q_i}{\sum_i^n \frac{d_i}{d_{prox}}}$$

$$v_a^{pref} = \frac{d_{avg}}{d_{prox}} v_{avg} + \frac{d_{prox} - d_{avg}}{d_{prox}} v_{goal}$$



- To be noted: when there's no valid velocity, agent remains its current velocity



# METRICS

- total number of collisions during the entire experiment
- computation time per frame,
- total time to solve the problem,
- average ratio of respected proximity links per frame,
- and number of successful runs.

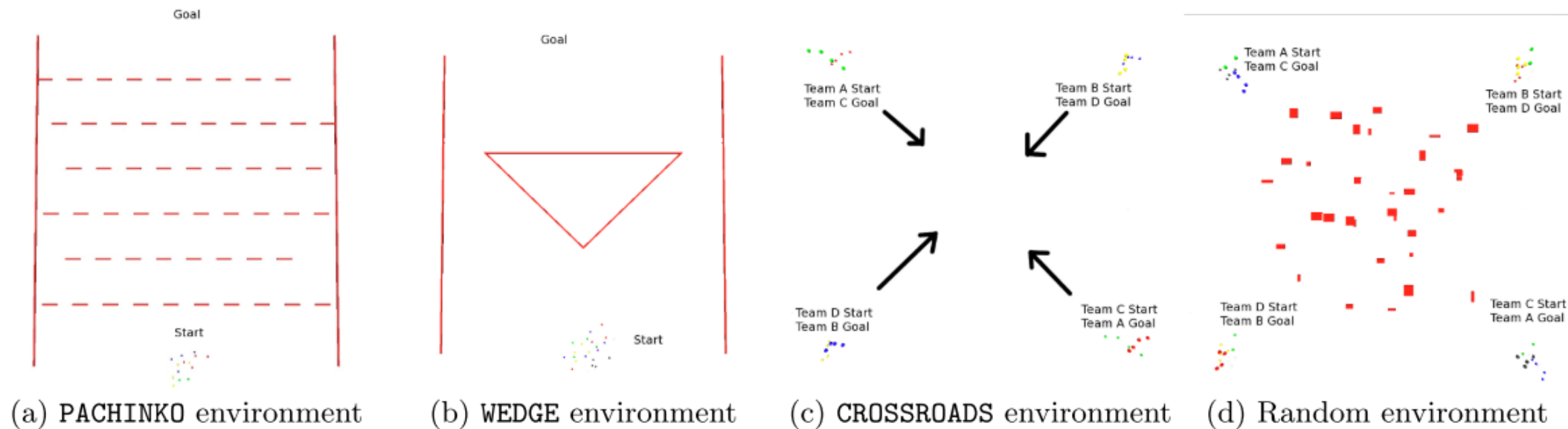
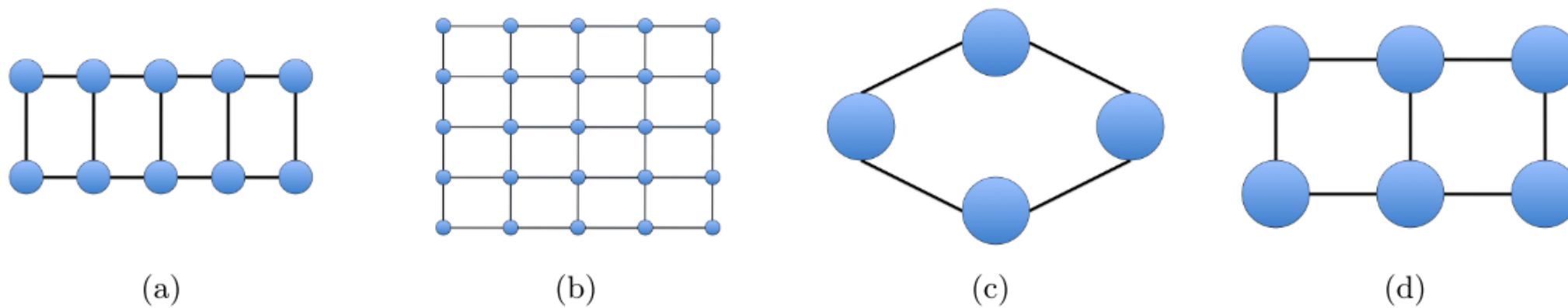


Figure 7: The environments on which the experiments were executed



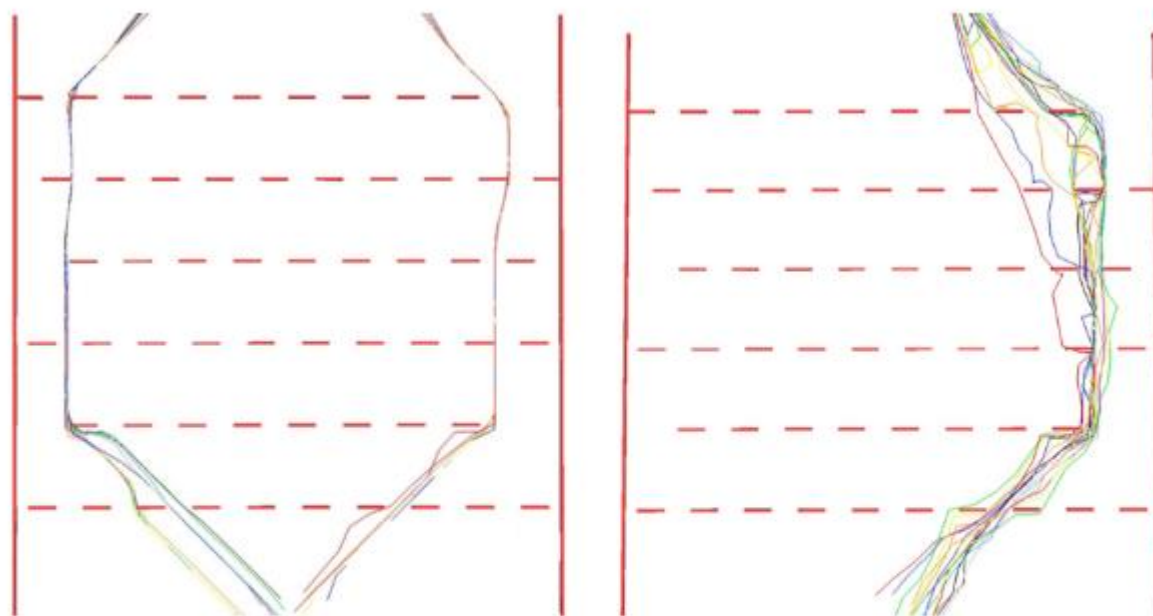


Figure 10: An example of the paths taken by 24 agents in the PACHINKO environment for the RVO (left) and LOCO (right) approach.

# PRIORITIZED GROUP NAVIGATION WITH FORMATION VELOCITY OBSTACLES [2015 ICRA]

- Purpose
  - navigating a group of robots having prioritized formations amidst static and dynamic obstacles. At each planning cycle, we compute a **new** formation which accounts for both these **priority** values and the **safe** progress of the robots towards their goals.
- Methodology
  - Group planning\* (main discussion, novelty)
    - To find  $F^*$  which balances between user's input and collision-free progress
  - Individual planning
    - Slightly discussed

# INFERENCE

$$\alpha_1 \begin{matrix} \triangle \\ \triangle \\ \triangle \\ \triangle \end{matrix} + \alpha_2 \begin{matrix} \triangle \\ \triangle \\ \triangle \\ \triangle \end{matrix} + \mathcal{N}(0, \sigma^2) = \begin{matrix} \triangle & & \triangle \\ & \triangle & \\ & & \triangle \end{matrix}$$

Fig. 1. **Defining Arbitrary Formations** We can decompose any arbitrary formation into a linear combination of the user provided template formations  $T$  plus some noise. For example, the staggered formation on the far right is a combination of the line-abreast and column formations with  $a_1 = 0.56$  and  $a_2 = 0.43$ , respectively, and  $\sigma = 0.08$ .

- Given a formation  $F$ , cost function is defined as:  $E(F) = p_F (\mathbf{v}_F \cdot \hat{\mathbf{v}}^{\text{pref}})$
- To obtain a formation  $F^*$  from set of  $F$ s, it's assumed to be a convex combination of  $k$  provided templates with noise.

$$F = a_1 T_1 + \dots + a_k T_k + \mathcal{N}(0, \sigma^2), \text{ s.t. } \sum_{i=1}^k a_i = 1,$$

- Infer the value of priority of formation  $F$ .

$$p_F = a_1 p_1 + a_2 p_2 + \dots + a_k p_k - \gamma \sigma,$$

- Infer the value set given the formation  $F$ .

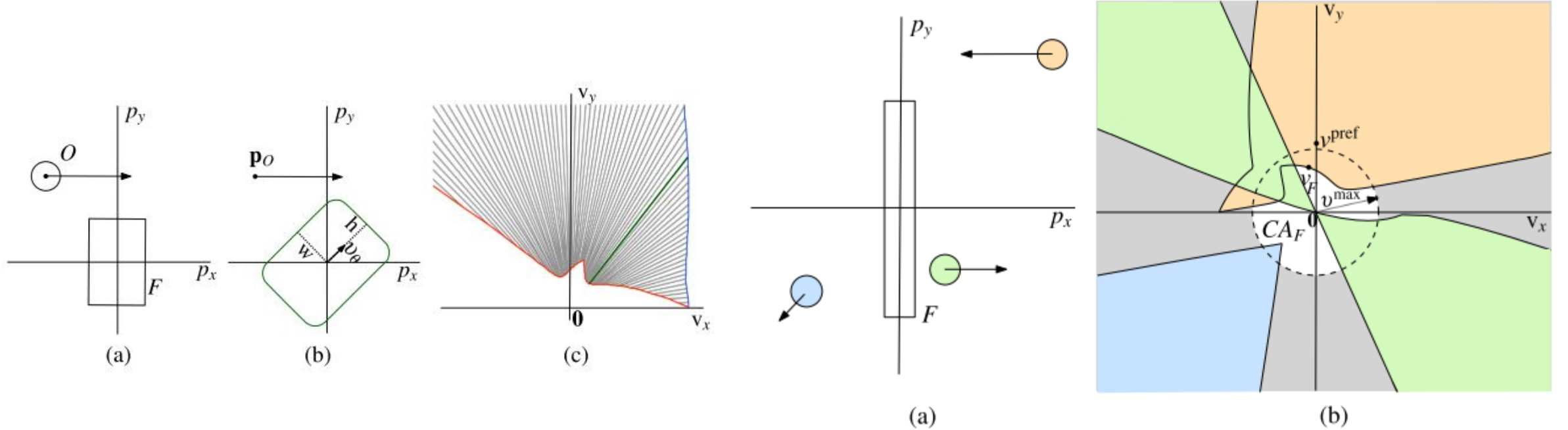
$$\begin{aligned} & \operatorname{argmax}_{a_1, \dots, a_k, \sigma} P(a_1, \dots, a_k, \sigma | F) \\ & = \operatorname{argmax}_{a_1, \dots, a_k, \sigma} \mathcal{L}(F | a_1, \dots, a_k, \sigma) + \mathcal{L}(a_1, \dots, a_k) + \mathcal{L}(\sigma), \end{aligned} \quad (7)$$

$$\operatorname{argmax}_{a_1, \dots, a_k, \sigma} \frac{-[D(F, a_1 T_1 + \dots + a_k T_k)]^2}{\sigma^2}.$$

where  $\mathcal{L}(\cdot)$  denotes the *log likelihood* function.

# FORMATION VELOCITY OBSTACLE

- Treat formation as a bounding box with  $w$  and  $h$ .



- Tuning  $\gamma$

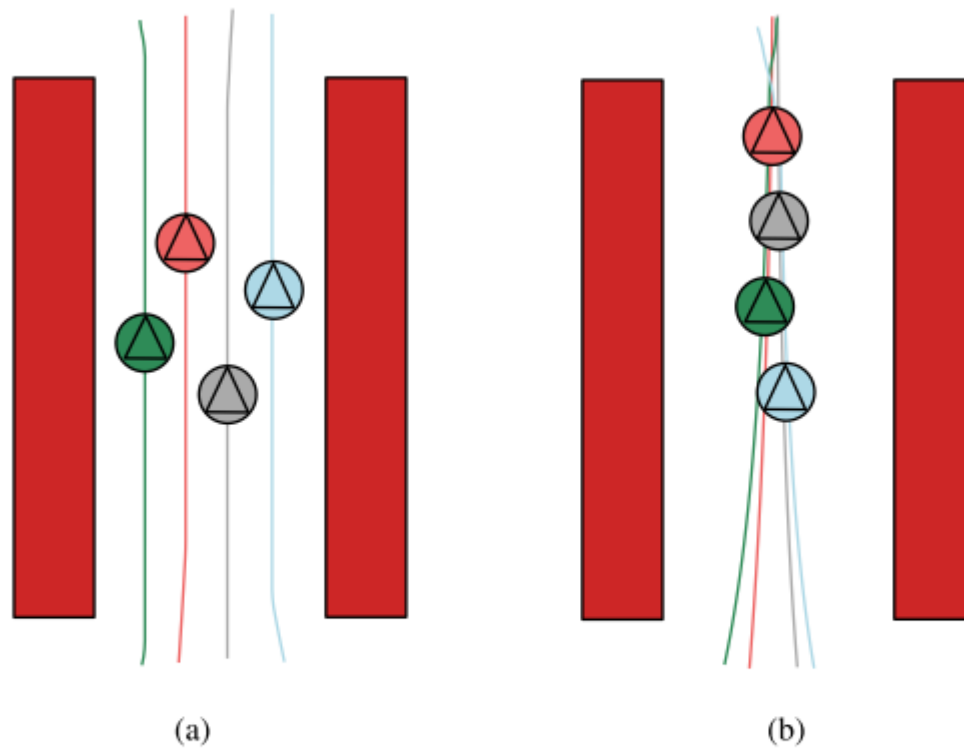
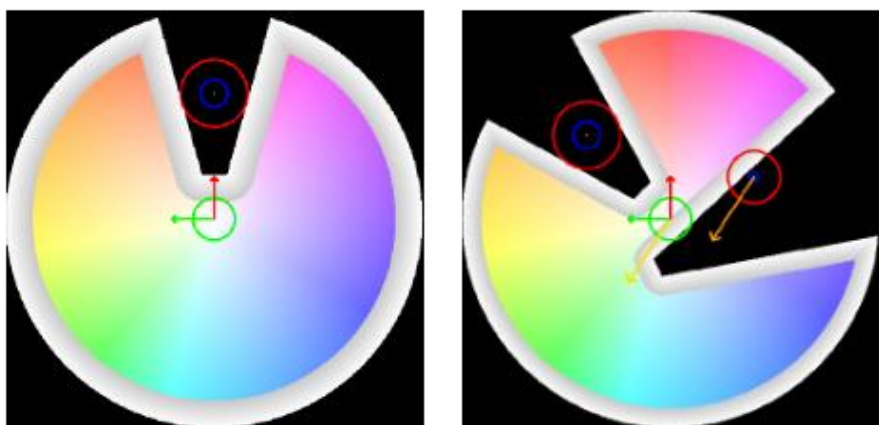


Fig. 6. **Effect of  $\gamma$  parameter.** Agents navigate through a passage given two formations: line abreast and single column. (a) With a small value of  $\gamma$  agents adopt an ad-hoc formation which fits the obstacle. (b) With a larger value of  $\gamma$  agents follow very closely the single column formation.



# AN ADAPTIVE VELOCITY OBSTACLE AVOIDANCE ALGORITHM FOR AUTONOMOUS SURFACE VEHICLES [2019 IROS]

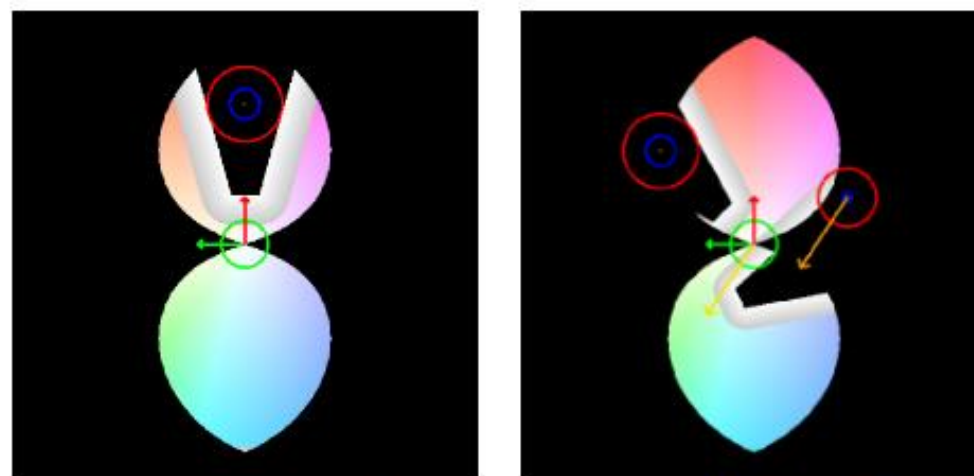
- Purpose
  - A real-time obstacle avoidance for surface vehicle with protective zone concept, using particle swarm optimization to minimize a multicriteria evaluation metric(danger, deviation and cross distance)
- Methodology
  - Protective Zone



(a) Single static obstacle.

(b) Static and dynamic obstacles.

Kinematics constraint



(a) Single static obstacle.

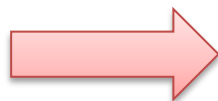
(b) Static and dynamic obstacles.

# VELOCITY SELECTION

- Multicriteria optimization object function  $h(V)$

$$\min_{\Delta v_d, \Delta \theta_d, \nabla_i} h(V_i)$$

$$h(V_i) = \varepsilon^T \cdot \psi$$



PSO

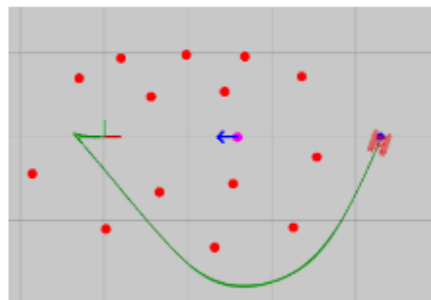


$$V_i = \varphi_1 \cdot V_{i-1} + \varphi_2 \cdot r_1 \cdot (pBest - P_{i-1}) + \varphi_3 \cdot r_2 \cdot (gBest - P_{i-1}) + \varphi_4 \cdot \tau$$

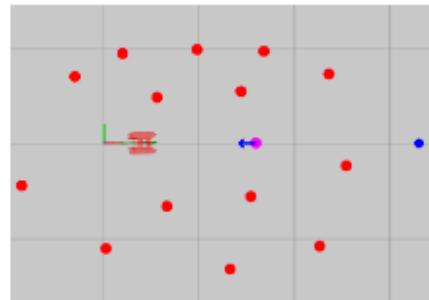
$$P_i = P_{i-1} + V$$

$$\varepsilon = \begin{bmatrix} |\Delta v_d| \\ |\Delta \theta_d| \\ \nabla_i \end{bmatrix}, \Delta v_d, \Delta \theta_d \in [-1, 1], \nabla_i \in [0, 1]$$

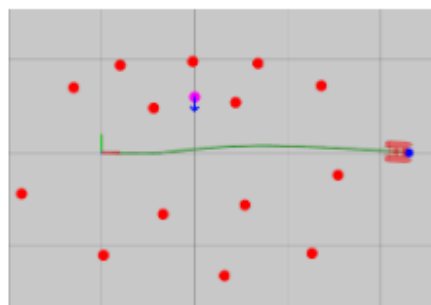
# RESULT



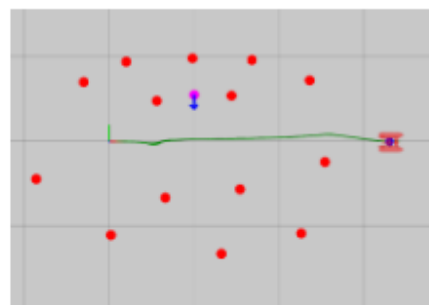
(a) AVOA (Scenario A).



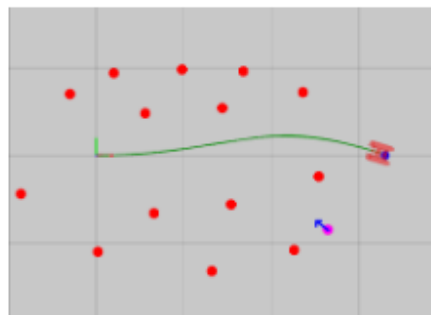
(b) TEB (Scenario A).



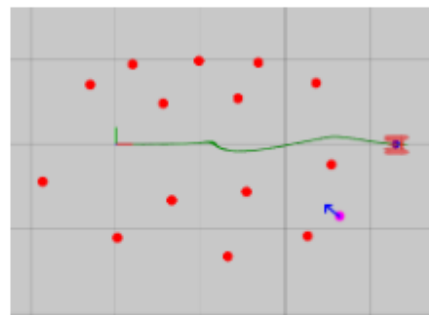
(c) AVOA (Scenario B).



(d) TEB (Scenario B).



(e) AVOA (Scenario C).



(f) TEB (Scenario C).



# DISTRIBUTED LYAPUNOV-BASED MODEL PREDICTIVE CONTROL FOR COLLISION AVOIDANCE OF MULTI-AGENT FORMATION

- Navigate groups of robots in a shared environment while maintaining segregation among groups.
  - Extended concept of RVO with flocking behaviors and hierarchical abstractions.

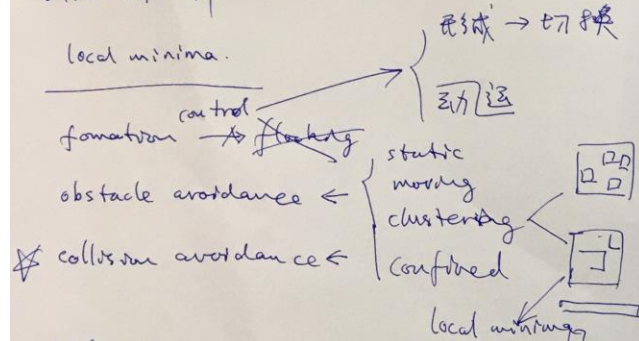
# ARRANGEMENT

## Q&A

不再发散 → 收敛

文档 →

创新点/故事



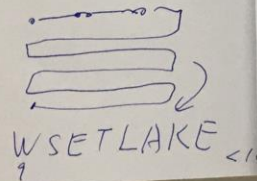
引文:

- control law:
- ① CA: 引文, RVO
- OA: VO + ...

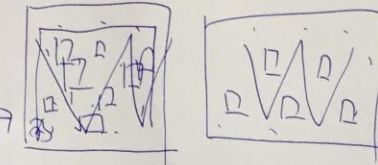
描述  
框图

结果: ① CA + 形式  
好例子.

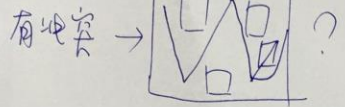
WEST LAKE



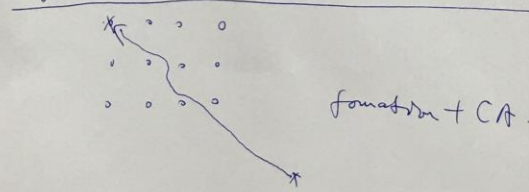
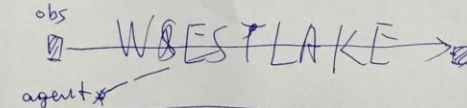
② 形成 + CA + OA (静)



无冲突

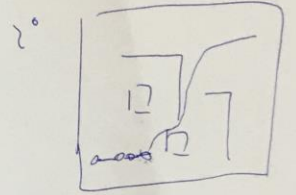


③ formation + CA + OA 引文



④ moving + CA + OA

$$W \begin{matrix} \square & \square \\ \square & \square \end{matrix} \rightarrow W$$



下面: ① 引文总结

② 结果 大量仿真

③ 写  
引文号 → 引文号 ← 引文号 → 引文号

③



**THANK YOU**

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WESTLAKE UNIVERSITY